

Grade 7 Common Core Vocabulary

A Story of Ratios

Grade 7 - Module 2

Properties of Operations and Integer Vocabulary

Properties of Operations

- **Additive Inverse** - the opposite of a number on the number line
- the number and its additive inverse have a sum of 0
Example: the additive inverse (opposite) of -3 is 3.
- **Additive Identity** - zero is the additive identity.
- zero can be added to other numbers without changing their value

Examples: $12 + 0 = 12$

$$x + 0 = x$$

$$6y + 0 = 6y$$

- **Associative Property** – in addition and multiplication, no matter how the numbers are grouped, the answer will always be the same

EXAMPLE:

$$(4 + 2) + 6 = 6 + 6 = 12$$

$$4 + (2 + 6) = 4 + 8 = 12$$

- **Commutative Property** – in addition and multiplication, numbers may be added or multiplied together in any order

Example:

$$6 + 2 = 8 \text{ and } 2 + 6 = 8$$

$$3 \times 2 = 6 \text{ and } 2 \times 3 = 6$$

- **Distributive Property** - multiplying a number is the same as multiplying its addends by the number, then adding the products

Example: $3(5 + 6)$

$$3 \cdot 5 + 3 \cdot 6$$

- **Multiplicative Inverse** - numbers whose product is 1 are multiplicative inverses of one another.

Example: $\frac{3}{4}$ and $\frac{4}{3}$ are multiplicative inverses of one another because $\frac{3}{4} \times \frac{4}{3} = \frac{4}{3} \times \frac{3}{4} = 1$.

Multiplicative inverses do not always have to be the reciprocal.

Example: $\frac{1}{5}$ and $\frac{10}{2}$ both have a product of 1, which makes them multiplicative inverses.

- **Multiplicative Identity Property** — any number time 1 equals itself
The *multiplicative identity* is 1.
Example: $12 \cdot 1 = 12$
 $a \cdot 1 = a$
 $6x \cdot 1 = 6x$
- **Absolute Value** – the distance the number is from zero on the number line
Example: $|-5| = 5$
- **Credit** – money returned to an account, the opposite of a debit
- **Debit** – money deducted from a related bank account or taken out of the account
- **Deposit** – the act of putting money into a bank account
- **Distance Formula** - the length between two points or objects
If p and q are rational numbers on a number line, then the distance between p and q is $|p - q|$.
- **Integer** - positive numbers, negative numbers, or zero but not fractions or decimals
- whole numbers and their opposites
 $\{\dots, -3, -2, -1, 0, 1, 2, 3, \dots\}$
- **Inverse** - opposite
- **Loss** – a decrease in amount, as when the money earned is less than the money spent
- **Opposites** – two numbers that are the same distance from zero on a number line
- additive inverses
Example: -4, +4
- **Positives** – numbers greater than zero
- **Profit** - a gain
- the positive difference between the money earned and spent
- **Negatives** - any number less than zero written with a minus sign
- **Withdraw** – to take money out of a bank account

Vocabulary that means subtract

debit
withdraw
positive
loss

Vocabulary that means add

credit
deposit
negative
profit

Some examples are from:

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Grade 7 - Module 2

Rational Number Vocabulary

- **Rational Numbers** - numbers that can be written as the ratio of two integers with a non-zero Denominator
- all integers, fractions, repeating decimals and terminating decimals
- **Repeating Decimal** - the decimal form of a rational number, for example, $\frac{1}{3} = 0.\overline{3}$
- **Terminating Decimal** - a decimal is called terminating if the decimal ends and does not repeat
- **Complex Fraction**— fraction with a fraction in the numerator, denominator, or both
Example: $\frac{\frac{1}{2}}{3}$, $\frac{2}{\frac{1}{4}}$, $\frac{\frac{1}{2}}{\frac{3}{4}}$
- **Multiplicative Identity Property** – any number time 1 equals itself
The *multiplicative identity* is 1.
Example: $12 \cdot 1 = 12$
 $a \cdot 1 = a$
 $6x \cdot 1 = 6x$
- **Multiplicative Inverse** - numbers whose product is 1 are multiplicative inverses of one another.
Example: $\frac{3}{4}$ and $\frac{4}{3}$ are multiplicative inverses of one another because $\frac{3}{4} \times \frac{4}{3} = \frac{4}{3} \times \frac{3}{4} = 1$.
Multiplicative inverses do not always have to be the reciprocal.
Example: $\frac{1}{5}$ and $\frac{10}{2}$ both have a product of 1, which makes them multiplicative inverses.

Grade 7 - Module 1

Proportional Relationships Vocabulary

- **Ratio** – a comparison of two quantities which may be written as a to b, a:b or as a fraction $\frac{a}{b}$

Example:

four to six, 4 to 6, 4:6 or $\frac{4}{6}$

- **Rate** – a ratio with different units of measurement

Example: births per year, cost per pound, words per minute, miles per hour

- **Unit Rate** - comparison of two measurements (rate) in which the second term is 1

Common Unit Rates: dollars per hour, miles per hour, heartbeats per minute

Example: If Nancy earns \$180 in 20 hours, then the unit rate is

$$\$180 / 20 \text{ hours} = \$9 \text{ per hour}$$

- **Equivalent Ratios** - ratios with the same value

Equivalent ratios are made by multiplying or dividing the numerator and the denominator by the same non-zero number.

Equivalent Ratios

| Michelle | Erik | Equivalent |
|--|--|---|
| $\frac{48}{64} \div \frac{16}{16} = \frac{3}{4}$ | $\frac{72}{96} \div \frac{24}{24} = \frac{3}{4}$ | $\frac{3}{4} = \frac{3}{4} \rightarrow \frac{48}{64} = \frac{72}{96}$ |

Examples:

- **Ratio Table** – a table that shows a comparison of two quantities

Example:

Ratio Table

| <i>Sugar</i> | <i>Flour</i> |
|--------------|--------------|
| 2 | 3 |
| 4 | 6 |
| 6 | 9 |

- **Proportional** – being in proportion means that two ratios or fractions are of equal value.

Example: $1:3 = 2:6$ so they are in proportion,

$\frac{1}{2} = \frac{2}{4}$ so they are in proportion.

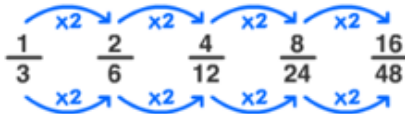
(A visual is on the next page.)

proportion

Equivalent fractions or ratios are in proportion because they are of equal value.



Proportional fractions are made by multiplying the numerator and the denominator by the same number.



Proportional ratios are made by multiplying all the terms in the ratio by the same number.



Ratio: Lemonade Recipe



Mix cups of water, lemon juice and sugar in the ratio 3:1:1.

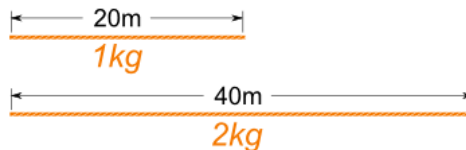
| | | | | | |
|-------------|---|---|----|----|----|
| Water | 3 | 6 | 12 | 24 | 48 |
| Lemon Juice | 1 | 2 | 4 | 8 | 16 |
| Sugar | 1 | 2 | 4 | 8 | 16 |

In this table, the terms have been doubled each time.

- **Proportional Relationship** - When two quantities always have the same size in relation to each other. In other words they have the same ratio.

Example: When 20m of rope weighs 1kg, then:

- 40m of that rope weighs 2kg
- 200m of that rope weighs 10kg



- **Constant of Proportionality** - the constant ratio between two quantities

If x is proportional to y , then $k = y/x$. k = the constant of proportionality.

The constant of proportionality can never be zero.

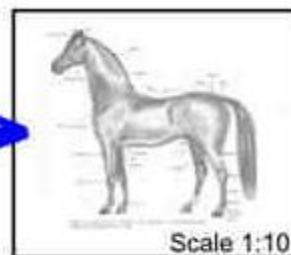
Example: If the ratio of y to x is 2 to 3, then the constant of proportionality, k , is $\frac{2}{3}$ and $y = \frac{2}{3}x$

- **Scale Drawing** - A drawing that shows a real object with **accurate sizes reduced or enlarged** by a certain amount

Example:



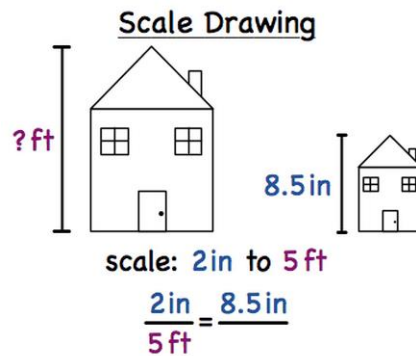
Real Horse
1500 mm high



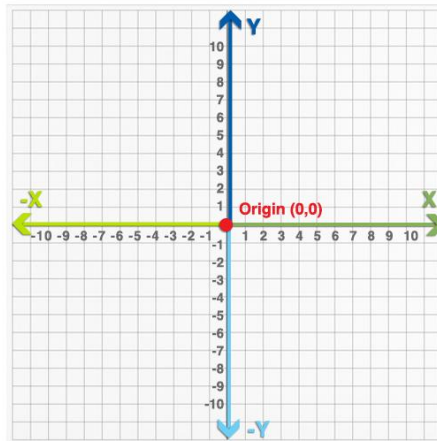
Drawn Horse
150 mm high

- **Scale Factor** –the ratio of measurement of the drawing compared to the measurement of the original figure

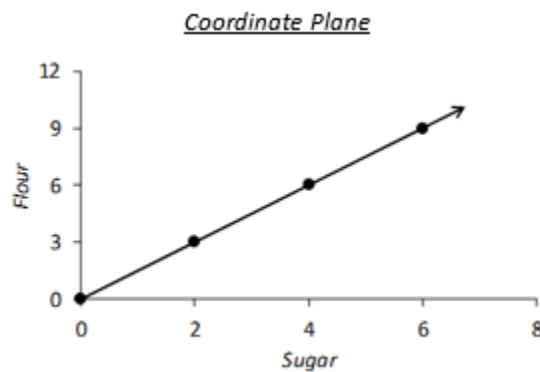
Example:



- **Coordinate Plane** - a plane containing two perpendicular axes (x and y) intersecting at a point called the origin (0,0)



- Graphs with equations in the form of $y = kx$
 - Example:



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Grade 7 - Module 3

Expressions and Equations Vocabulary

- **Term** - one part of an algebraic expression which may be a number, variable, or product of both
Example: 8, x, 2a

terms in algebraic expressions

| Expression | Terms |
|------------------------|--------------------------------|
| $2a + b^2$ | $2a$ and b^2 |
| $4x^3 + 3xz - 5$ | $4x^3$, $3xz$ and 5 |
| $9x^3 + 5x^3 + x + 16$ | $9x^3$, $5x^3$, x and 16 |

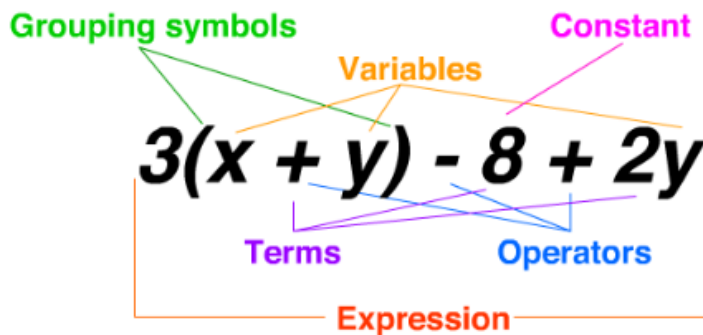
- **Variable** - a letter that represents a number
Example: n in $10 + n$
- **Coefficient** - a number which multiplies a variable
Examples:

3 is the **coefficient** in $3x$

4 is the **coefficient** in $4y^2$

- **Expression** - one or a group of terms and may include variables, constants, and operations

parts of an expression



\neq

expressions DO NOT contain
equality or inequality signs

$>$ $<$

- **Numerical Expression** - only numbers and operations

Examples:

$$\boxed{6} \quad \boxed{6 + 6} \quad \boxed{6 + 6 - 3}$$

- **Algebraic Expression** – contains at least one variable

Examples:

$$\boxed{6x^2} \quad \boxed{6x + 6}$$

- **Equivalent Expressions** - two algebraic expressions are said to be equivalent if their values are the same when substituting the values of the variables are same

Example: $3(x + 3)$ and $3x + 9$ are equivalent expressions, for $x = 4$

$$3(x + 3) = 3x + 9$$

$$3(4 + 3) = 3x + 9$$

$$3(7) = 3 \cdot 4 + 9$$

$$21 = 12 + 9$$

$$21 = 21$$

- **Equation** - a mathematical statement containing an equals sign, to show that two expressions are equal

parts of an equation

$$5x^2 + 2x - 8 = 16$$

- **Factor** - a whole number that divides exactly into another number

Example: Factors of 15 are 1, 3, 5, 15.

- **Greatest Common Factor** - the largest number that two or more other numbers are divisible by

One way to determine GCF:

1. List the factors for each number. $\left[\begin{array}{l} 24 \text{ 1, 2, 3, 4, 6, 8, 12, 24} \\ 36 \text{ 1, 2, 3, 4, 6, 9, 12, 18, 36.} \end{array} \right.$

2. List the common factors.
(the ones they both have) 1, 2, 3, 4, 6, 12

3. Circle the greatest common factor. 1, 2, 3, 4, 6, 12
 $\text{GCF} = 12$

- **An Expression in Expanded Form** - An expression that is written as sums (and/or differences) of products whose factors are numbers, variables, or variables raised to whole number powers
A single number, variable, or a single product of numbers and/or variables is also considered to be in expanded form.

Example: $2a + 3b + 2c + 6a - b + 4c$ is in expanded form

- **An Expression in Standard Form** - An expression that is in expanded form where all like terms have been collected

Example: $8a + 2b + 6c$ is in standard form

- **An Expression in Factored Form** - An expression that is a product of two or more expressions

Example: $2(6a + b + 3c)$ is in factored form

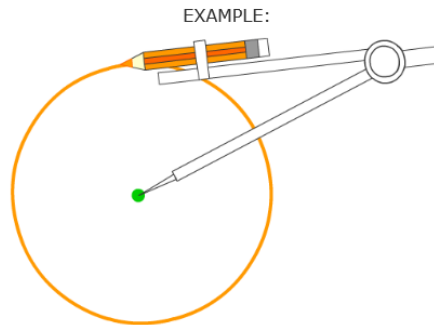
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Grade 7 - Module 3

Circle Vocabulary

- **Circle** - a shape formed by the set of all points which are the same distance from the center



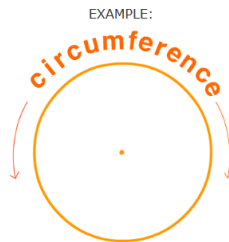
- **Diameter of a Circle** – a line segment that passes through the center of a circle whose endpoints lie on the circle.

diameter is twice the radius or $d = 2r$

- **Radius** – a line segment connecting the center of a circle and a point on the circle
- half the diameter or $r = d/2$

- **Circumference** – distance around a circle

Circumference = diameter times pi or $C = \pi d$



- **Area** – number of square units to cover a surface

Area of circle = πr^2

- **Pi** - the irrational number *pi*, denoted π

$\pi = \frac{\text{circumference}}{\text{diameter}}$

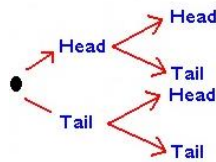
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Grade 7 - Module 5

Probability Vocabulary

- **Probability** - a number between 0 and 1 that represents the likelihood that an outcome will occur.
- **Compound event** - an event consisting of more than one outcome from the sample space of a chance experiment.
- **Tree diagram** - a way of representing the outcomes of an experiment that consists of a sequence of steps, such as flipping a coin twice



- **Theoretical Probability** – a comparison of favorable outcomes to the number of possible equally likely outcome
Example:
From the letters A, E, I, O, U the theoretical probability of selecting the letter E is $\frac{1}{5}$.
- **Experimental Probability** - The number of times the outcome occurs compared to the total number of trials.
Example: If a coin lands on heads three times out of five flips then the experimental probability is $\frac{3}{5}$.
- **Simulation** - the process of generating “artificial” data that are consistent with a given probability model

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Grade 7 - Module 5

Statistics Vocabulary

- **Random sample** - a group selected in a way that gives every different possible sample of the same size an equal chance of being selected
- **Inference** - using data from a sample to draw conclusions about a population.
- **Measures of center** – mean, median, mode

Mean - the total of all the scores or amounts, divided by how many scores there were
- also called the average

Example: $\frac{\text{sum of the numbers}}{\text{how many number were added}}$

| | |
|---------------|--------------------|
| Monday | 35° |
| Tuesday | 30° |
| Wednesday | 32° |
| Thursday | 29° |
| Friday | 27° |
| Saturday | 37° |
| Sunday | 34° |
| Total: | <u>224°</u> |
| Divide | $224^\circ \div 7$ |
| Mean: | $= 32^\circ$ |

Median - the middle value of an ordered set of data values

Example:

How to determine the median in a set of values.

Order the values from least to greatest.
Locate the middle value.

3, 4, 5, 5, 5, 6, 6, 7, 8, 8, 9

If the number of values is even, the median is the
average of the two middle values.

Mode - the value that occurs the most in a set of data values

Example:

How to determine the mode in a set of scores.

Order the scores from least to greatest.
Locate the score that occurs the most.

3, 4, 5, 5, 5, 6, 6, 7, 8, 8, 9

mode = 5

3, 4, 5, 5, 5, 6, 6, 6, 8, 8, 9

modes = 5 and 6

two modes are called bimodal

- **Measures of variability** –refers to how spread out a group of data is
 - measures how much your scores differ from each other
 - the most frequently used measures are the standard deviation and range

Range - is the difference between the largest and smallest values

Example: take this set of numbers: 13, 18, 13, 14, 13, 16, 14, 21, 13

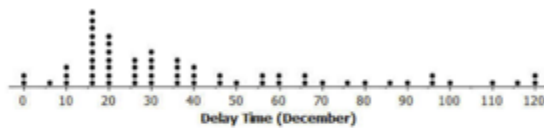
The largest value in the list is 21, and the smallest is 13,
so the range is $21 - 13 = 8$.

- **Mean absolute deviation (MAD)** - the mean of the distances of each value from the mean of the set of data values

Three steps to calculate:

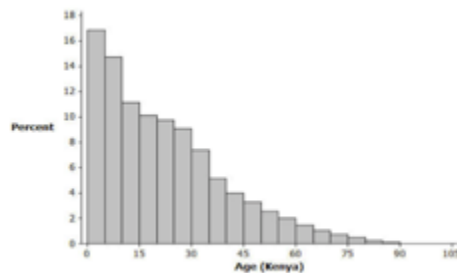
1. Find the **mean** of all values.
2. Find the **distance** of each value from that mean (subtract the mean from each value, ignore negative signs).
3. Then find the **mean of those distances**.

- **Dot plots** (see example below)



Dot Plot

- **Histograms** (see example below)



Histogram

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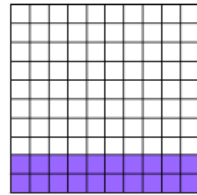
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Grade 7 - Module 4

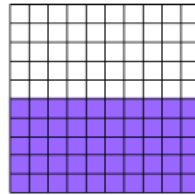
Percent Vocabulary

- **Percent** - is a fraction expressed as a number out of 100 followed by the % symbol

Examples: $\frac{20}{100} = 20\%$, $\frac{50}{100} = 50\%$, $\frac{1}{2} = 50\%$



$$\frac{20}{100} = 20\%$$



$$\frac{50}{100} = 50\%$$

- **Discount** - a reduction in the normal price
- **Discount Price** – the lower price once the discount is subtracted
- **Original Price** – beginning price
- **Commission** - a fee paid for services, usually a percentage of the total cost
Example: Jack's Gallery sold Amanda's painting for \$500,
so Amanda paid them a 10% commission which was \$50.
- **Gratuuity (tip)** – a fancy word for a tip
- a gift of money for service, as to a waiter or hairdresser
Example: A tip or gratuity is the amount of money a customer at a restaurant pays to the server in addition to the cost of the meal.
- **Tax** – money that the government collects based on income, sales, etc.
Example: Alex earned \$300 but had to pay \$42 of that to the government as tax.
- **Markup** - the amount added by a seller to the original cost to create a new higher selling price
Example: If the original cost is \$4.00 and the markup is 25%,
then the sales price should be $\$4.00 + \$4.00 \cdot \frac{25}{100} = \5.00 .

A faster way - to calculate the sale price is to make the original cost equal to 100%.

The markup is 25% so the sales price is 125% of the original cost.

In the example, $\$4.00 \cdot \frac{125}{100} = \5.00 .

- **Absolute Error** – given the exact value x of a quantity and an approximate value a of it, the absolute error is $|a - x|$
- **Percent Error** - the percent the absolute error is of the exact value

Example:

$\left(\frac{|a-x|}{|x|}\right)(100\%)$, where x is the exact value, and a is an approximate value

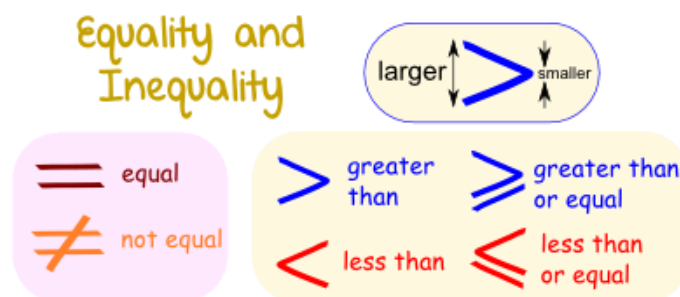
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Grade 7 - Module 3

Inequality Vocabulary

- **Inequality** – two values that are not equal
- opposite to equality



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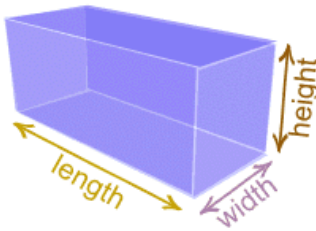
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Grade 7 - Module 6

Surface Area/Volume Vocabulary

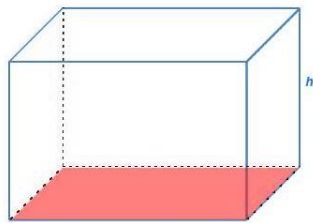
- **Right rectangular prism** - a prism with two identical, rectangular bases

Example:



- **Surface of a Prism** – side of the prism

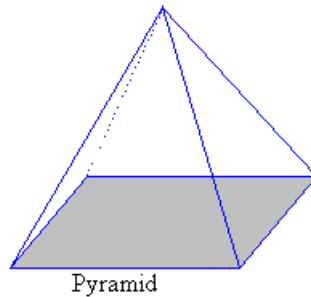
Example: one surface of the prism is red as shown below



- **Right rectangular pyramid**

- a three- dimensional figure with four faces that are triangles and a base that is a rectangle

Example:



Some examples are from:

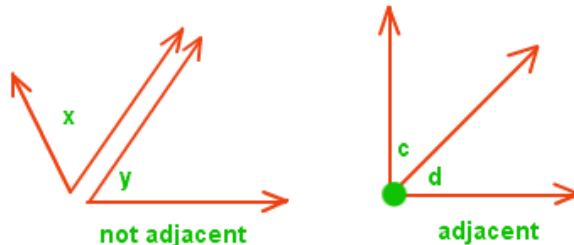
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Grade 7 - Module 6

Angle Pairs Vocabulary

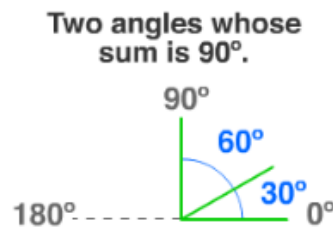
- **Adjacent angles** – two angles with a shared vertex and side (ray)

Example:



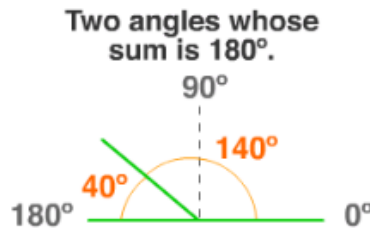
- **Complementary angles** - two angles whose sum is 90°

Example: 30° and 60°



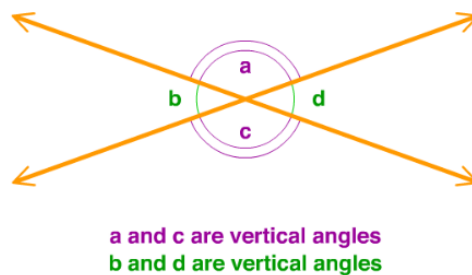
- **Supplementary angles** – two angles whose sum is 180°

Example: 40° and 140°



- **Vertical Angles** - pair of angles directly opposite each other, formed by the intersection of straight lines and may also be called opposite angles

Example:



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Grade 7 - Module 6

Triangle Vocabulary

- **Identical (Congruent) Triangles** - if there are corresponding angles of equal measure and corresponding sides of equal length
- **Three sides condition** - side, side, side method
 - all three pairs of corresponding sides of a triangle are equal length
- **Two angles and the included side condition** – angle, side, angle method
 - two pairs of corresponding angles and the included side of one triangle have equal measures
- **Two sides and the included angle condition** – side, angle, side method
 - two pairs of corresponding sides and the included angle of the triangle are equal measure